An OCaml Implementation of Binary Sessions

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Abstract

In this chapter we describe FuSe, a simple OCaml module that implements binary sessions and enables a hybrid form of session type checking without resorting to external tools or extensions of the programming language. The approach combines static and dynamic checks: the former ones are performed at compile time and concern the structure of communication protocols; the latter ones are performed as the program executes and concern the linear usage of session endpoints. We recall the minimum amount of theoretical background for understanding the essential aspects of the approach (Section 11.1) and then describe the API of the OCaml module throughout a series of simple examples (Section 11.2). In the second half of the chapter we detail the implementation of the module (Section 11.3) and discuss a more complex and comprehensive example, also arguing about the effectiveness of the hybrid approach with respect to the early detection of protocol violations (Section 11.4). We conclude with a survey of closely related work (Section 11.5).

The source code of FuSe, which is partially described in this chapter and can be used to compile and run all the examples given therein, can be downloaded from the second author’s home page.
11.1 An API for Sessions

We consider the following grammar of types and session types

\[
\begin{align*}
t, s & ::= \text{bool} \mid \text{int} \mid \alpha \mid T \mid \{l_i : t_i\}_{i \in I} \mid \cdots \\
T, S & ::= \text{end} \mid !t.T \mid ?t.T \mid \&\{l_i : T_i\}_{i \in I} \mid \odot\{l_i : T_i\}_{i \in I} \mid A \mid \overline{A}
\end{align*}
\]

where types, ranged over by \( t \) and \( s \), include basic types, type variables, session types, disjoint sums, and possibly other (unspecified) types. Session types, ranged over by \( T \) and \( S \), comprise the usual constructs for denoting depleted session endpoints, input/output operations, branches and choices, as well as possibly dualized session type variables \( A, B, \) etc.

The dual of a session type \( T \), written \( \overline{T} \), is obtained as usual by swapping input and output operations and is defined by the following equations:

\[
\begin{align*}
\overline{A} &= A \\
\overline{\text{end}} &= \text{end} \\
\overline{(!t.T)} &= ?t.T \\
\overline{(?t.T)} &= !t.T \\
\overline{\&\{l_i : T_i\}_{i \in I}} &= \odot\{l_i : T_i\}_{i \in I} \\
\overline{\odot\{l_i : T_i\}_{i \in I}} &= \&\{l_i : T_i\}_{i \in I}
\end{align*}
\]

Following Gay and Vasconcelos [4], our aim is to incorporate binary sessions into a (concurrent) functional language by implementing the API shown in Table 11.1. The \texttt{create} function creates a new session and returns a pair with its two peer endpoints with dual session types. The \texttt{close} function is used to signal the fact that a session is completed and no more communications are supposed to occur in it. The \texttt{send} and \texttt{receive} functions are used for sending and receiving a message, respectively: \texttt{send} sends a message of type \( \alpha \) over an endpoint of type \( !\alpha.A \) and returns the same endpoint with its type changed to \( \overline{A} \) to reflect that the communication has occurred; \texttt{receive} waits for a message of type \( \alpha \) from an endpoint of type \( ?\alpha.A \) and returns a pair with the message and the same endpoint with its type changed to \( A \). The \texttt{branch} and \texttt{select} functions deal with sessions that may continue along different paths of interaction, each path being associated with a label \( 1_i \). Intuitively, \texttt{select} takes a label \( 1_k \) and an endpoint of type \( \odot\{l_i : A_i\}_{i \in I} \)

Table 11.1 Application programming interface for binary sessions

<table>
<thead>
<tr>
<th>Function</th>
<th>Signature</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{create}</td>
<td>\texttt{unit \rightarrow A \times \overline{A}}</td>
</tr>
<tr>
<td>\texttt{close}</td>
<td>\texttt{end \rightarrow unit}</td>
</tr>
<tr>
<td>\texttt{send}</td>
<td>\texttt{\alpha \rightarrow !\alpha.A \rightarrow A}</td>
</tr>
<tr>
<td>\texttt{receive}</td>
<td>\texttt{?\alpha.A \rightarrow \alpha \times A}</td>
</tr>
<tr>
<td>\texttt{select}</td>
<td>\texttt{(A_k \rightarrow {l_i : A_i}<em>{i \in I}) \rightarrow \odot{l_i : A_i}</em>{i \in I} \rightarrow A_k}</td>
</tr>
<tr>
<td>\texttt{branch}</td>
<td>\texttt{&amp;{l_i : A_i}<em>{i \in I} \rightarrow {l_i : A_i}</em>{i \in I} \rightarrow A_k}</td>
</tr>
</tbody>
</table>
where \( k \in I \), sends the label over the endpoint and returns the endpoint with its type changed to \( A_k \), which is the continuation corresponding to the selected label. The most convenient Ocaml representation for labels is as functions that \( \text{inject} \) an endpoint (say, of type \( A_k \)) into a disjoint sum \( \{1_i : A_i\}_{i \in I} \) where \( k \in I \). This explains the type of \( \text{select} \)'s first argument. Dually, \( \text{receive} \) waits for a label from an endpoint of type \( \&\{1_i : A_i\}_{i \in I} \) and returns the continuation endpoint injected into a disjoint union.

We note a few more differences between the API we implement in this chapter and the one described by Gay and Vasconcelos [4]. First of all, we use parametric polymorphism to give session primitives their most general type. Second, we have a single function \( \text{create} \) to initiate a new session instead of a pair of \( \text{accept}/\text{request} \) functions to synchronize a service and a client. Our choice is purely a matter of simplicity, the alternative API being realizable on top of the one we present (the API implemented in the FuSe distribution already provides for the \( \text{accept}/\text{request} \) functions, which we will see at work in Section 11.4). Finally, our communication primitives are \( \text{synchronous} \) in that output operations block until the corresponding receive is performed. Again, this choice allows us to provide the simplest implementation of these primitives solely using functions from the standard Ocaml library. Asynchronous communication can be implemented by choosing a suitable communication framework.

### 11.2 A Few Simple Examples

Before looking at the implementation of the communication primitives, we illustrate the API at work on a series of simple examples. In doing so, we assume that the API is defined in a module named \( \text{Session} \). The following code implements a client of an “echo” service, a service that waits for a message and bounces it back to the client.

```ocaml
let echo_client ep x =
  let ep = Session.send x ep in
  let res, ep = Session.receive ep in
  Session.close ep;
  res
```

The parameter \( ep \) has type \(!\alpha.??\beta.\text{end}\) and \( x \) has type \( \alpha \). The function \( \text{echo\_client} \) starts by sending the message \( x \) over the endpoint \( ep \). The construction \( \text{let} \) rebinds the name \( ep \) to the endpoint returned by the primitive \( \text{send} \), which now has type \( ?\beta.\text{end} \). The endpoint is then used for receiving a
message of type $\beta$ from the service. Finally, `echo_client` closes the session and returns the received message.

The service is implemented by the `echo_service` function below, which uses the parameter `ep` of type $?\alpha. !\alpha.\text{end}$ to receive a message `x` and then to send it back to the client before closing the session.

```ocaml
let echo_service ep =
  let x, ep = Session.receive ep in
  let ep = Session.send x ep in
  Session.close ep
```

There is an interesting asymmetry between (the types of) client and service in that the message `x` sent by the service is the very same message it receives, whereas the message `res` received by the client does not necessarily have the same type as the message `x` it sends. Indeed, there is nothing in `echo_client` suggesting that `x` and `res` are somewhat related. This explains the reason why the session type of the endpoint used by the client ($!\alpha. ?\beta. \text{end}$) is more general than that used by the service ($?\alpha. !\alpha.\text{end}$) aside from the fact that the two session types describe protocols with complementary actions. In particular, $!\alpha. ?\beta. \text{end}$ is not dual of $?\alpha. !\alpha.\text{end}$ according to the definition of duality given earlier: in order to connect client and service, $\beta$ must be unified with $\alpha$. The code that connects `echo_client` and `echo_service` through a session is shown below:

```ocaml
let _ =
  let a, b = Session.create () in
  let _ = Thread.create echo_service a in
  print_endline (echo_client b "Hello, world!")
```

The code creates a new session, whose endpoints are bound to the names `a` and `b`. Then, it activates a new thread that applies `echo_service` to the endpoint `a`. Finally, it applies `echo_client` to the remaining endpoint `b`.

We now wish to generalize the `echo` service so that a client may decide whether to use the service or to stop the interaction without using it. A service that offers these two choices is illustrated below:

```ocaml
let opt_echo_service ep =
  match Session.branch ep with
  | `Msg ep → echo_service ep
  | `End ep → Session.close ep
```

In this case the service uses the `branch` primitive to wait for a label selected by the client. We use OCaml’s polymorphic variant tags (`\`Msg and
A Few Simple Examples

End in this case) as labels because they do not have to be declared explicitly, unlike data constructors of plain algebraic data types. The initial type of \( ep \) is now \( \&[\text{End} : \text{end}, \text{Msg} : ?\alpha. !\alpha. \text{end}] \) and the value returned by \texttt{branch} has type \([\text{End} : \text{end}, \text{Msg} : ?\alpha. !\alpha. \text{end}] \). In the \texttt{Msg} branch the service behaves as before. In the \texttt{End} branch the service closes the session without performing any further communication.

The following function realizes a possible client for \texttt{opt_echo_service}:

\begin{verbatim}
let opt_echo_client ep opt x =
  if opt then
    let ep = Session.select (fun x -> `Msg x) ep
    in echo_client ep x
  else
    let ep = Session.select (fun x -> `End x) ep
    in Session.close ep; x
\end{verbatim}

This function has type \( \&[\text{End} : \text{end}, \text{Msg} : !\alpha. ?\alpha. \text{end}] \rightarrow \text{bool} \rightarrow \alpha \rightarrow \alpha \) and its behavior depends on the boolean parameter \( opt \): when \( opt \) is \texttt{true}, the client selects the label \texttt{Msg} and then follows the same protocol as \texttt{echo_client}; when \( opt \) is \texttt{false}, the client selects the label \texttt{End} and then closes the session. Note that we have to \( \eta \)-expand the polymorphic variant tags \`Msg\) and \`End so that their type matches that expected by \texttt{select}. When the same label is used several times in the same program, it is convenient to define the \( \eta \)-expansion once, for example as

\begin{verbatim}
let _Msg x = `Msg x
let _End x = `End x
\end{verbatim}

Note also that the messages sent and received now have the same type in the initial type of \( ep \). This is because of the structure of \texttt{opt_echo_client}, which returns either \( x \) or the message returned by the service.

A further elaboration of the echo service allows the client to send an arbitrary number of messages before closing the session. In order to describe this protocol we must extend the syntax of session types presented earlier to permit recursive types. In practice, the representation of session types we will choose in Section 11.3 allows us to describe recursive protocols by piggybacking on OCaml’s support for equi-recursive types, which is enabled by passing the \texttt{-rectypes} option to the compiler. The implementation of the elaborated echo service is therefore a straightforward recursive function:

\begin{verbatim}
let rec rec_echo_service ep =
  match Session.branch ep with
\end{verbatim}
```ocaml
| `Msg ep \rightarrow let x, ep = Session.receive ep in
  let ep = Session.send x ep in
  rec_echo_service ep |
| `End ep \rightarrow Session.close ep |
```

Note the recursive call `rec_echo_service ep` in the `Msg` branch, which allows the server to accept again a choice from the client after replying back to a request. The `rec_echo_service` function now expects an endpoint `ep` of type `rec A&[End : end, Msg : \?\alpha . !\alpha . A]` where `rec AT` denotes the (equi-recursive) session type `T` in which occurrences of `A` stand for the session type itself.

The following client

```ocaml
let rec rec_echo_client ep =
  function |
  [] \rightarrow let ep = Session.select _End ep in
  Session.close ep; [] |
  | x :: xs \rightarrow let ep = Session.select _Msg ep in
  let ep = Session.send x ep in
  let y, ep = Session.receive ep in
  y :: rec_echo_client ep xs
```

has type `rec A&[End : end, Msg : !\alpha . ?\beta . A] \rightarrow list \alpha \rightarrow \beta list` and repeatedly invokes the recursive echo service on each element of a list.

### 11.3 API Implementation

In order to implement the API presented and used in the previous sections we have to make some choices regarding the OCaml representation of session types and of session endpoints. In doing so we have to take into account the fact that OCaml’s type system is not substructural and therefore is unable to statically check that session endpoints are used linearly. In the rest of this section we address these concerns and then detail the implementation of the API in Table 11.1.

**Representation of session types.** FuSe relies on the encoding of session types proposed by Dardha et al. [1] and further refined by Padovani [13]. The basic idea is that a sequence of communications on a session endpoint can be compiled as a sequence of one-shot communications on linear channels.
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(channels used exactly once) where each exchanged message carries the actual payload along with a continuation, namely a (fresh) channel on which the subsequent communication takes place.

The image of the encoding thus relies on two types:

- a type $\emptyset$ which is not inhabited, and
- a type $\langle \rho, \sigma \rangle$ which describes channels for receiving messages of type $\rho$ and sending messages of type $\sigma$. Both $\rho$ and $\sigma$ can be instantiated with $\emptyset$ to indicate that no message is respectively received and/or sent.

The correspondence between session types $T$ and types of the form $\langle t, s \rangle$ is given by the map $\llbracket \cdot \rrbracket$ defined below

<table>
<thead>
<tr>
<th>Encoding of session types</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\llbracket \text{end} \rrbracket = \langle \emptyset, \emptyset \rangle$</td>
</tr>
<tr>
<td>$\llbracket ? t . T \rrbracket = \langle \llbracket t \rrbracket \times \llbracket T \rrbracket, \emptyset \rangle$</td>
</tr>
<tr>
<td>$\llbracket ! t . T \rrbracket = \langle \emptyset, \llbracket t \rrbracket \times \llbracket T \rrbracket \rangle$</td>
</tr>
<tr>
<td>$\llbracket &amp; [1_i : T_i]<em>{i \in I} \rrbracket = \langle [1_i : \llbracket T_i \rrbracket]</em>{i \in I}, \emptyset \rangle$</td>
</tr>
<tr>
<td>$\llbracket @ [1_i : T_i]<em>{i \in I} \rrbracket = \langle \emptyset, [1_i : \llbracket T_i \rrbracket]</em>{i \in I} \rangle$</td>
</tr>
<tr>
<td>$\llbracket A \rrbracket = \langle \rho_A, \sigma_A \rangle$</td>
</tr>
<tr>
<td>$\llbracket A \rrbracket = \langle \sigma_A, \rho_A \rangle$</td>
</tr>
</tbody>
</table>

and extended homomorphically to all types. We assume that for each session type variable $A$ there exist two distinct type variables $\rho_A$ and $\sigma_A$ that are also different from any other type variable $\alpha$.

For example, the session type $? \alpha . A$ is encoded as $\langle \alpha \times \langle \rho_A, \sigma_A \rangle, \emptyset \rangle$, which describes a channel for receiving a message of type $\alpha \times \langle \rho_A, \sigma_A \rangle$ consisting of a component of type $\alpha$ (that is the actual payload of the communication) and a component of type $\langle \rho_A, \sigma_A \rangle$ (that is the continuation channel on which the rest of the communication takes place). There is a twist in the encoding of outputs for the session type of the continuation is dualized. The reason for this is that the type associated with the continuation channel in the encoding describes the behavior of the receiver of the continuation rather than that of the sender. As we will see, this twist provides us with a simple way of expressing duality relations between session types, even when they are (partially) unknown. The encodings of $\@ [1_i : T_i]_{i \in I}$ and $\& [1_i : T_i]_{i \in I}$ follow the same lines and make use of polymorphic variant types to represent the selected or received choice. As an example, the encoding of $T = \@ [\text{End} : \text{end}, \text{Msg} : ! \alpha . ? \beta . \text{end}]$ is computed as follows
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\[ T \] = \langle 0, \langle \text{ End } : \text{[end]} \rangle, \text{Msg} : \text{[?\alpha . !\beta . end]} \rangle
= \langle 0, \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \text{[!\beta . end]} \rangle \rangle
= \langle 0, \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \langle 0, \beta \times \text{[end]} \rangle \rangle \rangle
= \langle 0, \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \langle 0, \beta \times \langle 0, 0 \rangle \rangle \rangle \rangle

If instead we consider the session type \( \overline{T} = \&[\text{End : end}, \text{Msg} : \text{?\alpha . !\beta . end}] \), then we derive:

\[ \overline{T} \] = \langle \langle \text{ End } : \text{[end]} \rangle, \text{Msg} : \text{[?\alpha . !\beta . end]} \rangle \rangle
= \langle \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \text{[!\beta . end]} \rangle \rangle \rangle
= \langle \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \langle 0, \beta \times \text{[end]} \rangle \rangle \rangle \rangle
= \langle \langle \text{ End } : \langle 0, 0 \rangle \rangle, \text{Msg} : \langle \alpha \times \langle 0, \beta \times \langle 0, 0 \rangle \rangle \rangle \rangle \rangle

Remarkably we observe that the encoding of \( \overline{T} \) can be obtained from that of \( T \) by swapping the two components of the resulting channel types. This is a general property:

**Theorem 1** If \( \langle T \rangle = \langle t, s \rangle \), then \( \overline{T} \) = \( \langle s, t \rangle \).

An equivalent way of expressing this result is the following: if \( \langle T \rangle = \langle t_1, t_2 \rangle \) and \( \langle S \rangle = \langle s_1, s_2 \rangle \), then

\( T = S \iff \langle T \rangle = \langle S \rangle \iff t_1 = s_2 \wedge t_2 = s_1 \)

meaning that the chosen encoding allows us to reduce session type duality to type equality. This property holds also for unknown or partially known session types. In particular, \( \langle A \rangle = \langle \rho_A, \sigma_A \rangle \) and \( \overline{\langle A \rangle} = \langle \sigma_A, \rho_A \rangle \).

We end the discussion of session type representation with two remarks. First, although the representation of session types chosen in FuSe is based on the continuation-passing encoding of sessions into the linear \( \pi \)-calculus [1], we will implement the communication primitives in FuSe so that only the payload (or the labels) are actually exchanged. Therefore, the semantics of FuSe communication primitives is consistent with that given in [4] and the components corresponding to continuations in the above types are solely used to relate the types of session endpoints as these are passed to, and returned from, FuSe communication primitives. Second, the OCaml type system is not substructural and there is no way to qualify types of the form \( \langle t, s \rangle \) as linear, which is a fundamental requirement for the type safety of the API. We will overcome this limitation by means of a mechanism that detects linearity violations at runtime. Similar mechanisms have been proposed by Tov and Pucella [20] and by Hu and Yoshida [5].
Table 11.2  OCaml interface of the API for binary sessions

```ocaml
module Session : sig
  type 0
  type (ρ, σ) st (* OCaml syntax for ⟨ρ, σ⟩ *)
  val create : unit → (ρ, σ) st × (σ, ρ) st
  val close : (0, 0) st → unit
  val send : α → (0, (α × (σ, ρ) st)) st → (ρ, σ) st
  val receive : ((α × (ρ, σ) st), 0) st → α × (ρ, σ) st
  val select : ((σ, ρ) st → α) → (0, [>] as α) st → (ρ, σ) st
  val branch : ([>] as α, 0) st → α
end
```

Having chosen the representation of session types, we can see in Table 11.2 the OCaml interface of the module that implements the binary session API. In OCaml syntax, the type ⟨t, s⟩ is written (t, s) st. There is a direct correspondence between the signatures of the functions in Table 11.2 and those shown in Table 11.1 so we only make a couple of remarks. First, we extensively use Theorem 1 whenever we need to refer to a session type and its dual. This can be seen in the signatures of create, send and select where both (ρ, σ) st and (σ, ρ) st occur. Second, in the types of select and branch the syntax [>] as α means that α can only be instantiated with a polymorphic variant type. Without this constraint the signatures of select and branch would be too general and the API unsafe: it would be possible to receive a label sent with select, or to branch over a message sent with send. Note that the constraint imposed by [>] as α extends to every occurrence of α in the same signature.

By comparing Tables 11.1 and 11.2 it is clear that the encoding makes session types difficult to read. This problem becomes more severe as the protocols become more involved. The distribution of FuSe includes an auxiliary tool, called rosetta, that implements the inverse of the encoding to pretty print encoded session types into their familiar notation. The tool can be useful not only for documentation purposes but also to decipher the likely obscure type error messages issued by OCaml. Hereafter, when presenting session types inferred by OCaml, we will often show them as pretty printed by rosetta for better clarity.

**Representation of session endpoints.** Session primitives can be easily implemented on top of any framework providing channel-based communications. FuSe is based on the Event module of OCaml’s standard library, which
provides communication primitives in the style of Concurrent ML [16] and the abstract type \( t \) \( \text{Event.channel} \) for representing channels carrying messages of type \( t \). It is convenient to wrap the \( \text{Event} \) module so as to implement \textit{unsafe communication channels}, thus:

```ocaml
module UnsafeChannel : sig
  type t
  val create : unit \to t
  val send : \alpha \to t \to unit
  val receive : t \to \alpha
end = struct
  type t = unit \text{Event.channel}
  let create = \text{Event.new_channel}
  let send x u = \text{Event.sync} (\text{Event.send} u (\text{Obj.magic} x))
  let receive u = \text{Obj.magic} (\text{Event.sync} (\text{Event.receive} u))
end

We just need three operations on unsafe channels, \textit{create}, \textit{send} and \textit{receive}. The first one creates a new unsafe channel, which is simply an \textit{Event} channel for exchanging messages of type \textit{unit}. The choice of \textit{unit} over any other OCaml type is immaterial: the messages exchanged over a session can be of different types, hence the type parameter we choose here is meaningless because we will perform unsafe cast at each communication. These casts cannot interfere with the internals of the \textit{Event} module because \( t \text{Event.channel} \) is parametric on the type \( t \) of messages and therefore the operations in \textit{Event} cannot make any assumption on their content. The implementation of \textit{send} and \textit{receive} on unsafe channels is a straightforward adaptation of the corresponding primitives of the \textit{Event} module. Observe that, consistently with the communication API of Concurrent ML, \textit{Event.send} and \textit{Event.receive} do not perform communications themselves. Rather, they create \textit{communication events} which occur only when they are synchronized through the primitive \textit{Event.sync}. The \textit{Obj.magic} function from the standard OCaml library has type \( \alpha \to \beta \) and performs the necessary unsafe casts.

We now have all the ingredients for giving the concrete representation of (encoded) session types. This representation is kept private to the FuSe module so that the user can only manipulate session endpoint through the provided API:
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A session type is represented as a record with two fields: the `chan` field is a reference to the unsafe channel on which messages are exchanged; the `mutable valid` field is a boolean flag that indicates whether the endpoint can be safely used or not. Every operation that uses the endpoint first checks whether the endpoint is valid. If this is the case, the `valid` flag of the endpoint is reset to `false` so that any subsequent attempt to reuse the same endpoint can be detected. Otherwise, an `InvalidEndpoint` exception is raised. It is convenient to encapsulate this functionality in an auxiliary function `use`, which is private to the module and whose implementation is shown below:

```
let use u =
  if u.valid then u.valid ← false
  else raise InvalidEndpoint
```

In principle, checking that the `valid` field is `true` and resetting it to `false` should be performed atomically, to account for the possibility that several threads are attempting to use the same endpoint simultaneously. In practice, since OCaml’s scheduler is not preemptive and `use` allocates no memory, the execution of `use` is guaranteed to be performed atomically in OCaml’s runtime environment. Different programming languages might require a more robust handling of the validity flag [13].

Whenever an operation on a session endpoint completes and the session endpoint is returned, its `valid` flag should be set to `true` again. Doing so on the existing record, though, would be unsafe. Instead, a new record referring to the very same unsafe channel must be created. Again it is convenient to provide this functionality as a private, auxiliary function `fresh`:

```
let fresh u = { u with valid = true }
```

**Implementation of communication primitives.** A new session is initiated by creating a new unsafe channel `ch` and returning the two peer endpoints of the session, which both refer to the same channel. The `valid` flag of each peer is set to `true`, indicating that it can be safely used:

```
let create () = let ch = UnsafeChannel.create ()
  in { chan = ch; valid = true },
  { chan = ch; valid = true }
```
The implementation of close simply invalidates the endpoint. OCaml’s garbage collector takes care of any further finalization that may be necessary to clean up the corresponding unsafe channel:

```
let close = use

let send x u =
  use u; UnsafeChannel.send x u.chan; fresh u
let receive u =
  use u; (UnsafeChannel.receive u.chan, fresh u)
```

The send operation starts by checking that the endpoint is valid and, in this case, invalidates it. Then, the message x is transmitted over the underlying unsafe channel and a refreshed version of the endpoint is returned. The receive operation is analogous, except that it returns a pair containing the message received from the underlying unsafe channel and the refreshed endpoint:

```
let select = send
let branch u =
  use u; UnsafeChannel.receive u.chan (fresh u)
```

The select operation is behaviorally equivalent to send, since its purpose is to transmit the selected label (which is its first argument) over the channel. On the other hand the branch operation injects the refreshed session endpoint with the function received from the channel:

```
We conclude this section showing the type inferred by OCaml for the rec_echo_client defined in Section 11.1:

```
val recEcho : (0,\alpha) list \rightarrow (0,\beta) list
```

As expected, the type is rather difficult to understand. Part of this difficulty is a consequence of the fact that the type expression t as \alpha, which is used in OCaml also to denote a recursive type, is placed in a position such that t does not correspond to the encoding of a session type. It is only by unfolding this recursive type that one recovers an image of the encoding function. The same signature pretty printed by rosetta becomes

```
val recEcho : rec X. \{ End: end \rightarrow (0,\alpha) list \rightarrow (0,\beta) list \}
```

whose interpretation is straightforward.
11.4 Extended Example: The Bookshop

In this section we develop a FuSe version of a known example from the literature [4], where mother and child order books from an online bookshop. The purpose of the programming exercise is threefold. First, we see a usage instance of the accept and request primitives provided by FuSe for establishing sessions over service channels. Second, we discuss a non-trivial example in which the session types automatically inferred by OCaml are at the same time more general and more precise than those given by Gay and Vasconcelos [4]. This is made possible thanks to the support for parametric polymorphism and subtyping in session types that FuSe inherits for free from OCaml’s type system. Finally, we use the example to argue about the effectiveness of the FuSe implementation of binary sessions in detecting protocol violations, considering that FuSe combines both static and dynamic checks.

Service channels in FuSe are provided by the module Service, whose signature is shown below.

```ocaml
module Service : sig
  type α t
  val create : unit → α t
  val accept : (ρ, σ) st t → (ρ, σ) st
  val request : (ρ, σ) st t → (σ, ρ) st
  val spawn : ((ρ, σ) st → unit) → (ρ, σ) st t
end
```

The type A Service.t describe a service channel that allows initiation of sessions of type A. A session is created when two threads invoke accept and request over the same service channel. In this case, accept returns a session endpoint of type A and request returns its peer of type A.

The bookshop is modeled as a function that waits for session initiations on the service channel showAccess and invokes shopLoop at each connection:

```ocaml
let shop shopAccess =
  shopLoop (Service.accept shopAccess) []
```

A session initiated with the bookshop is handled by the function shopLoop, which operates over the established session endpoint s and the current list order of books in the shopping cart. The shopLoop function is recursive and repeatedly offers the possibility of adding a new book by selecting the Add label. When Checkout is selected instead, the bookshop
waits for a credit card number and an address and sends back an estimated
delivery date computed by an unspecified \( \text{deliveryOn} \) function.

\[
\text{let rec } \text{shopLoop } s \text{ order } = \\
\quad \text{match } \text{Session.branch } s \text{ with } \\
\quad | \text{'Add } s \rightarrow \\
\quad \quad \text{let } \text{book}, \ s = \text{Session.receive } s \text{ in} \\
\quad \quad \text{shopLoop } s \ (\text{book :: order}) \\
\quad | \text{'CheckOut } s \rightarrow \\
\quad \quad \text{let } \text{card}, \ s = \text{Session.receive } s \text{ in} \\
\quad \quad \text{let } \text{address}, \ s = \text{Session.receive } s \text{ in} \\
\quad \quad \text{let } s = \text{Session.send } (\text{deliveryOn order}) \ s \text{ in} \\
\quad \quad \text{Session.close } s
\]

The type inferred by OCaml for \( \text{shopLoop} \) is

\[
\text{val shopLoop : rec } \\
\quad \text{X.\&[ Add: } ?\alpha.X \ | \text{ CheckOut: } ?\beta.\gamma.\!\text{day.end } ] \\
\quad \rightarrow \alpha \text{ list } \rightarrow \text{unit}
\]

which is structurally the same given by Gay and Vasconcelos [4], except for
the type variables \( \alpha, \beta \) and \( \gamma \). Indeed, the body of \( \text{shopLoop} \) does not use the
received values \( \text{book}, \text{card} \) and \( \text{address} \) and therefore their type remains
generic.

We now model a mother process placing an order for two books, one
chosen by her and another selected by her son. In principle, the mother could
let the son select his own book by delegating the session with the bookshop
to him. However, the mother wants to be sure that her son will buy just one
book that is suitable for his age. To enforce these constraints, the mother
sends her son a voucher, that is a function providing a controlled interface
with the bookshop. Overall, the mother is modeled thus:

\[
\text{let mother card addr shopAccess sonAccess book } = \\
\quad \text{let } \text{c} = \text{Service.request } \text{shopAccess } \text{in} \\
\quad \text{let } \text{c} = \text{Session.select } \_\text{Add } \text{c in} \\
\quad \text{let } \text{c} = \text{Session.send } \text{book } \text{c in} \\
\quad \text{let } \text{s} = \text{Service.request } \text{sonAccess } \text{in} \\
\quad \text{let } \text{s} = \text{Session.send } (\text{voucher card addr c}) \ \text{s in} \\
\quad \text{Session.close } \text{s}
\]

where the parameters \( \text{card}, \text{addr} \) and \( \text{book} \) stand for information about
payment, delivery address and mother’s book. In addition, \( \text{shopAccess} \) and
sonAccess are the service channels for connecting with the bookshop and the son, respectively. The mother establishes a session \( c \) with the bookshop and adds \( \text{book} \) to the shopping cart. Afterwards, she initiates another session \( s \) for sending the voucher to her son. The voucher is modeled by the function:

\[
\text{let } \text{voucher} \ \text{card} \ \text{address} \ c \ \text{book} =
\text{let } c =
\begin{cases}
\text{if isChildrensBook book then} & \\
\text{let } c = \text{Session.select } _\text{Add} \ c \ \text{in} & \\
\text{Session.send } \text{book} \ c & \\
\text{else } c & \\
\end{cases}
\begin{cases}
\text{let } c = \text{Session.select } _\text{CheckOut} \ c \ \text{in} & \\
\text{let } c = \text{Session.send } \text{card} \ c \ \text{in} & \\
\text{let } c = \text{Session.send } \text{address} \ c \ \text{in} & \\
\text{let } \text{day}, c = \text{Session.receive } \ c \ \text{in} & \\
\text{Session.close } c & \\
\end{cases}
\]

where \( \text{book} \) is chosen by the son. If \( \text{book} \) is appropriate – something that is checked by the unspecified function \( \text{isChildrensBook} \) – the book is added to the shopping cart. Then, the order is completed and the connection with the bookshop closed.

For voucher and mother OCaml infers the following types:

\[
\begin{align*}
\text{val } \text{voucher} & : \alpha \to \beta \to \\
\text{rec } X. & \left[ \text{Add: } !\gamma.X \ | \ \text{CheckOut: } !\alpha. !\beta.?\delta.\text{end } \right] \\
& \to \gamma \to \text{unit} \\
\text{val } \text{mother} & : \alpha \to \beta \to \\
& \& \left[ \text{Add: } ?\gamma.\text{rec } X. \& \left[ \text{Add: } ?\delta.X \\
& | \ \text{CheckOut: } ?\alpha. ?\beta. !\epsilon.\text{end } \right] \\
& \right] \ Service.t \to ?(\delta \to \text{unit}).\text{end } \text{Service.t} \to \gamma \to \text{unit}
\end{align*}
\]

In contrast to the type of mother given by Gay and Vasconcelos [4], the type inferred by OCaml makes it clear that mother always adds at least one book to the shopping cart. The connection between mother and shopLoop is still possible because the protocol followed by mother is more deterministic than – or a supertype of [3] – the one she is supposed to follow.

To finish the exercise we model the son as the following function:

\[
\text{let } \text{son} \ \text{sonAccess} \ \text{book} =
\text{let } s = \text{Service.accept } \text{sonAccess} \ \text{in}
\]
An OCaml Implementation of Binary Sessions

```ocaml
let f, s = Session.receive s in
f book;
Session.close s
```

where `sonAccess` is the service channel used for accepting requests from his mother and `book` is the book he wishes to purchase. Note that the mother sends a function (obtained as the partial application of `voucher`) which is saturated by the son who provides the chosen book.

Overall, the code for connecting the three peers is shown below:

```ocaml
let _ =
  let mCard = "0123 4567 7654 3210" in
  let mAddr = "17 session type rd" in
  let mBook = "Life of Ada Lovelace" in
  let sBook = "1984" in
  let shopAccess = Service.create () in
  let sonAccess = Service.create () in
  let _ = Thread.create shop shopAccess in
  let _ = Thread.create (son sonAccess) sBook in
  mother mCard mAddr shopAccess sonAccess mBook
```

It is not possible to qualify session endpoints as linear resources in OCaml. This means that there are well-typed programs that, by using session endpoints non-linearly, cause communication errors and/or protocol violations. In the rest of this section we use the example developed so far to do some considerations concerning the effectiveness of the library in detecting programming errors involving session endpoints. In particular we argue that, despite the lack of linear qualification of session endpoints, OCaml’s type system is still capable of detecting a fair number of linearity violations. In the worst case, those violations that escape OCaml’s type checker are at least detected at runtime with the mechanism we have put in place in Section 11.3.

We can simulate a linearity violation by replacing the session endpoint bound by a `let` with `_`. For example, we can replace line 10 in the body of `voucher` with

```ocaml
let _ = Session.send address c in
```

so that the very same endpoint `c` is used both for this `send` and also for the subsequent `receive`. This linearity violation is detected by OCaml because the type of a session endpoint used for an output is incompatible (i.e., not unifiable) with that of an endpoint used for an input. Now suppose that we replace line 8 in the same function with
let _ = Session.select _CheckOut c in

so that the same endpoint c is used for both a select and the subsequent send. Even if select and send are both output operations, the type of messages resulting from the encoding of a plain message output has a topmost constructor which is incompatible with the polymorphic variant type resulting from the encoding of a label selection. Therefore, also this linearity violation is detected by OCaml's type checker. In general, any linearity violation arising from the use of different communication primitives is detected by OCaml. Consider then line 9, and suppose that we replace it with

let _ = Session.send card c in

so that the same endpoint c is used for sending both card and address. In this case the session endpoint is used for performing two plain outputs and the sent messages have compatible (i.e., unifiable) types. Therefore, taken in isolation, the voucher function would be well typed. In the context of the whole program, however, OCaml detects a type error also in this case. The point is that the faulty version of voucher now implements a different protocol than before. In particular, it appears as if voucher sends just one message after selecting CheckOut and before receiving the estimated delivery date. On the contrary, the protocol of the bookshop as implemented by shopLoop still expects to receive two messages before the delivery date is sent back to the client. Therefore, the protocols of the bookshop and the one inferred by the combination of mother and voucher are no longer dual to each other and the session request performed by mother to the bookshop is ill typed. For this problem to go undetected, there must be another linearity violation in the body of shopLoop, in the place that corresponds exactly to the point where the same violation occurs in voucher.

A simpler example of linearity violation that goes undetected by OCaml's type checker can be obtained by duplicating the f book application in the body of the son function. This modification might correspond either to a genuine programming error or to a malicious attempt of son to purchase more than one book. The reason why this duplication results into a linearity violation is that the closure corresponding to f contains the session endpoint c from mother, so applying f twice results in two uses of the same c. This error is detected by the type system of Gay and Vasconcelos [4] where the function f has a linear arrow type. In FuSe, the program compiles correctly, but the second application of f triggers the runtime mechanism that detects linearity violations causing the InvalidEndpoint exception to be raised.
11.5 Related Work

Several libraries of binary sessions have been proposed for different functional programming languages. Most libraries for Haskell [6, 12, 15, 17] use a monad that encapsulates the endpoints of open sessions. Besides being a necessity dictated by the lazyness of the language, the monad prevents programmers from accessing session endpoints directly thus guaranteeing that endpoint linearity is not violated. The monad also tracks the evolution of the type of session endpoints automatically, not requiring the programmer to rebind explicitly the same endpoint over and over again. However, the monad has a cost in terms of either expressiveness, usability, or portability: the monad defined by Neubauer and Thiemann [12] supports communication on a single channel only and is therefore incapable of expressing session interleaving or delegation. Pucella and Tov [15] propose a monad that stores a stack of endpoints (or, better, of their capabilities) allowing for session interleaving and delegation to some extent. The price for this generality is that the programmer has to write explicit monadic actions to reach the channel/capability to be used within the monad; also for this reason delegation is severely limited. Imai et al. [6] show how to avoid writing such explicit actions relying on a form of type-level computations. Lindley and Morris [9] describe another Haskell embedding of session types that provides first-class channels. Linearity is enforced statically using higher-order abstract syntax.

A different approach is taken in Alms [19, 21], a general-purpose programming language whose type system supports parametric polymorphism, abstract and algebraic data types, and built-in affine types as well. Tov [19] illustrates how to build a library of binary sessions on top of these features. Because Alms’ type system is substructural, affine usage of session endpoints is guaranteed statically by the fact that session types are qualified as affine. Further embeddings of session types in other experimental and domain-specific languages with substructural type systems have been described by Mazurak and Zdancewic [10], Lindley and Morris [8], and Morris [11].

Scalas and Yoshida [18] propose a library of binary session for Scala that is very related to our approach. As in FuSe, Scalas and Yoshida use a runtime mechanism to compensate for the lack of affine/linear types in Scala and work with the encoded representation of session types given by Dardha et al. [1]. A notable difference is that Scala type system is nominal, so that encoded session types are represented by Scala (case) classes which must be either provided by the programmer or generated from the protocol. This means that the protocol cannot be inferred automatically from the code and
that the subtyping relation between session types is constrained by the (fixed) subclassing relation between the classes that represent them.

The main source of inspiration for the representation of session types in FuSe originates from the continuation-passing encoding of binary sessions [1] and partially studied also in some earlier works [2, 7]. Our representation of encoded session types allows session type duality to be expressed solely in terms of type equality, whereas the representation chosen by Dardha et al. [1] requires a residual albeit simple notion of duality for the topmost channel type capability. Another difference is that we consider the encoding at the type level only, not requiring the explicit exchange of continuation channels for the implementation of communication primitives. For these reasons, the soundness of the encoding [1] cannot be used directly to argument about the soundness of FuSe’s typing discipline. Padovani [13] formalizes FuSe’s approach to binary sessions along with the necessary conditions under which the program does not raise exceptions. The same paper also illustrates a simple monadic API built on top of the primitives in Table 11.1 and investigates the overhead of the various approaches to linearity.

In addition to the features described in this chapter, FuSe supports sequential composition of session types. This feature makes it possible to describe with greater precision protocols whose set of (finite) traces is context-free as opposed to regular [14,22]. As discussed by Thiemann and Vasconcelos [22], these protocols arise naturally in the serialization of structured data types. Currently, FuSe provides the first and only implementation of context-free session type checking and inference.

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References


